## Time Value of Money Homework Exercise - KEY

Use the Time Value of Money tables to answer the following questions. Show your work!

1. You just purchased a house for $\$ 130,000$. Similar houses in your area are going up in value at a rate of $5 \%$ per year.
a. How much will your house be worth at the end of 15 years?

$$
\begin{array}{ll}
\mathrm{N}=15 & \text { Table } 1-\mathrm{FV} \text { of a Lump Sum } \\
\mathrm{I}=5 \% & \text { Factor for } 5 \%, 15 \text { years }=\mathbf{2 . 0 7 8 9} \\
\mathrm{PV}=\$ 130,000 & \\
\mathrm{PMT}=\$ 0 & \mathrm{FV}=\$ 130,000 \times 2.0789=\$ 270,257
\end{array}
$$

FV = ? ? = \$270,257
b. How much will it be worth at the end of 30 years?

$$
\begin{array}{ll}
\mathrm{N}=30 & \text { Table } 1-\mathrm{FV} \text { of a Lump Sum } \\
\mathrm{I}=5 \% & \text { Factor for 5\%, } 30 \text { years }=4.3219 \\
\mathrm{PV}=\$ 130,000 & \\
\mathrm{PMT}=\$ 0 & \mathrm{FV}=\$ 130,000 \times 4.3219=\$ 561,847 \\
\mathrm{FV}=? ?=\$ 561,847 &
\end{array}
$$

2. Your elderly neighbor just told you that he purchased his first new car for $\$ 1,500$ about 50 years ago. That has you wondering how much a new car will cost you when you are older. Car prices today average $\$ 20,000$. It appears that car prices increase at a rate of $6 \%$ every year. How much will a new car cost 50 years from today?

| $\mathbf{N}=50$ | Table 1 - FV of a Lump Sum |
| :---: | :---: |
| $\mathrm{I}=6 \%$ | Factor for 6\%, 50 years = 18.4202 |
| PV = \$20,000 |  |
| PMT = \$0 | FV = \$20,000 x 18.4202 = \$368,404 |

FV = ? ? = \$368,404 is the purchase price for a new car 50 years from now
3. You just won a prize!! The company that sponsored the prize will pay you $\$ 4,000$, but you won't get this $\$ 4,000$ until 3 years from today. Rather than waiting 3 years to collect this money, you are thinking of selling your rights to this prize to someone else so that you will receive some cash today. You can earn a return of $8 \%$ on your money. What is the lowest amount of money that you would sell your rights to this prize?

$$
\begin{array}{lc}
\mathrm{N}=3 & \text { Table 2-PV of a Lump Sum } \\
\mathrm{I}=8 \% & \text { Factor for } 8 \%, 3 \text { years }=0.7938 \\
\mathrm{PV}=? ?=\$ 3,175.20 \text { is the minimum price you would take } \\
\mathrm{PMT}=\$ 0 & \mathrm{PV}=\$ 4,000 \times 0.7938=\$ 3,175.20 \\
\mathrm{FV}=\$ 4,000 &
\end{array}
$$

4. What are the three main reasons that money has a time value?

Risk
Inflation RIO
Opportunity Cost
5. Your church wants to build a new community education center, so they have set a goal of collecting $\$ 250,000$ over the next 8 years to pay for the building. They can invest their money in account that earns $5 \%$ each year. They hope to collect contributions of $\$ 25,000 /$ year over the next 8 years. Will the church be able to reach their goal? (Assume BGN payments)

$$
\begin{array}{ll}
\mathrm{N}=8 & \text { Table } \mathbf{7}-\mathrm{FV} \text { of an Annuity } \\
\mathrm{I}=5 \% & \text { Factor for } 5 \%, 8 \text { years }=\mathbf{1 0 . 0 2 6 6} \\
\mathrm{PV}=\$ 0 & \\
\mathrm{PMT}=\$ \mathbf{2 5 , 0 0 0} & \mathrm{FV}=\$ 25,000 \times 10.0266=\$ 250,665 \\
\mathrm{FV}=? ?=\$ \mathbf{2 5 0 , 6 6 5} &
\end{array}
$$

Yes, they will be able to meet their goal because the FV is greater than the $\mathbf{\$ 2 5 0 , 0 0 0}$ goal.
6. Your grandparents started investing for your college tuition as soon as you were born. They invested $\$ 2,000 /$ year every year since you were born. Their college investment account earned a return of $7 \%$ each year. How much money will be in your college education account after 18 years of contributions?
(Assume BGN payments)

| $\mathrm{N}=18$ | Table $7-\mathrm{FV}$ of an Annuity |
| :--- | :--- |
| $\mathrm{I}=\mathbf{7 \%}$ | Factor for $\mathbf{7 \%}, 18$ years $=\mathbf{3 6 . 3 7 9 0}$ |
| $\mathrm{PV}=\mathbf{\$ 0}$ |  |
| $\mathrm{PMT}=\$ 2,000$ | $\mathrm{FV}=\mathbf{\$ 2 , 0 0 0} \times \mathbf{3 6 . 3 7 9 0}=\mathbf{\$ 7 2 , 7 5 8}$ |
| $\mathrm{FV}=? ?=\$ 72,758$ |  |

Your college education account will have $\mathbf{\$ 7 2 , 7 5 8}$ after 18 years of contributions by your grandparents. Thank you, grandparents!
7. Use the TVM Calculator spreadsheet to double-check your answers. List the answers to each question that you get from using the spreadsheet:
Question 1: a. \$270,260.66 b. \$561,852.51

Question 2: $\qquad$

Question 3: $\qquad$

Question 5: $\qquad$

Question 6: $\quad \$ 72,757.93$

