

Lesson 8 – Time Value of Money Take-Home Reading

Stop and think for a moment – what is the most powerful thing on Earth? Depending on whom you ask, you will get a variety of answers. A scientist might answer with “water, or maybe wind, or the atom.” A philosopher might say “time”. A religious person might say “faith.” An engineer will answer with, “leverage.” But someone familiar with financial principles will undoubtedly answer that question with the phrase, “time value of money.” But what exactly is time value of money (TMV)?

The phrase “time value of money” very simply refers to the fact that most people would rather at least some money in their hands today (“cash on the barrelhead”) rather than waiting to possibly receive a larger amount of money in the future. That is, money has a different value depending on the time that you receive it. Ask yourself this question, “Would you rather have \$90 of cash in your hands today or would you prefer to wait 1-2 years to receive \$100?” Most people would rather have \$100 than \$90 because it’s more money. The problem is that you have to wait to receive that \$100. And what can happen during that waiting period?

There are three main reasons that you might prefer to have the \$90 today instead of the \$100 in the future:

- Risk
- Inflation
- Opportunity Cost

An easy way to remember these three factors is the acronym “RIO”, as in Rio Grande. Risk is the easiest to remember – there is a risk that you will not receive the \$100 in the future. The person with whom you made the deal may have left town, or simply forgotten, or possibly he is bankrupt and cannot pay you the \$100. So, would you rather have \$90 in your hands today or wait to maybe receive \$100 in the future? You must think about the risks that are involved.

Inflation is a term that means that prices are increasing over time. Think about food prices. A cartful of groceries might cost \$90 today. But one year from now it might cost \$95. It’s the same groceries, but they cost more. This is called inflation. If you only had \$90 today you could purchase that cart of groceries. But 1 year from now if you had that same \$90 you would not be able to purchase that cart of groceries. This means that \$90 is more valuable to you today than \$90 one year from today – you can buy more with it today because of the rising prices over time.

The last term, “Opportunity Cost” can be a little confusing at first, but it’s a relatively easy concept. “Opportunity” means that you have possibilities for what you can do with that \$90 if you have it in hand today. You can spend it on something (like groceries); you can save it for emergencies; you can use it to pay down one of your loans; you can give it to someone (church, charity, gifts); or you can invest it to try to have more money in the future. These are your “opportunities” if you have the cash in hand today. The “Cost” part of the term indicates that there is a cost for using that \$90 for any of these opportunities. If you spend it, you cannot use it to pay down your debts or invest for the future. If you save it for emergencies, you can’t take advantage of lower prices by spending it today; and so on. In a nutshell, “opportunity cost” is what you are giving up by

using your money. Because you always want to use your money in the best way possible, we consider the opportunity cost to be the “next best use” of the money.

Here’s an example for Opportunity Cost. You just received \$1,000 as a graduation gift from your grandparents. To keep it simple, assume that you have the following options:

- keep it in your savings account where it earns 1% interest each year
- use it to pay down your car loan which has an interest rate of 5%

If you keep the money in your savings account, you will earn a 1% rate of return by the end of the year. But, if you use the money to pay down your car loan you will be saving yourself 5% this year. So, the opportunity cost of keeping the money in your savings account is roughly 5% - what you could have saved yourself by paying down your loan. If you use the money to pay down your loan, the opportunity cost is the 1% that you could have earned in your savings account. Which would you rather do, 1) earn 1% or 2) save 5%? Another way to ask this question is, “which option has the **lowest** opportunity cost?” You always want to use your money (or any asset) so that you have the lowest opportunity cost. That is, you want to use your money so that you give up the least amount possible. An easy way to remember this is that Opportunity Cost is a cost, and you always want to have the lowest costs possible.

Please note – it is hard to put a dollar value or percent return on many of the opportunities that you have for your money. For example, let’s look at two possibilities. Assume that you received \$1,000 from your grandparents. But in the first situation you have no money in your savings account. If you have a financial emergency (car breaks down, computer dies, etc.) you might have to get an emergency loan (possibly at a high interest rate) – and you don’t like to owe money to others. In the second situation you already have \$2,000 in your savings account, enough to cover most of your financial emergencies. This means that you can sleep much easier and you have fewer financial worries. It is hard to put a dollar value on what that “peace of mind” is worth from the first situation to the second situation.

So, RIO – Risk, Inflation, Opportunity Cost – are the main reasons that money is more valuable today than in the future. This is just another way of saying that you’d rather have a dollar in hand today rather than the promise of receiving a dollar in the future. That seems pretty simple. But why is this such a powerful force in the financial arena? The answer is “compound interest.” Compounding is a term that indicates how often the interest that you earn on an investment is converted into principal. When the interest that you earn is converted into principal, your money begins to snowball. You are “earning interest on interest.” Here’s an example – assume that you invest that \$1,000 you received from your grandparents into an account that will pay you 5% interest one time per year (we call this “annual compounding”) at the end of each year. After 1 year your account will be worth \$1,050:

\$1,000 of principal invested into the account
5% Interest rate (rate of return)

Interest earned in the first year = $\$1,000 \times 5\% = \50

Account value = \$1,000 of principal + \$50 of interest = \$1,050

Because you had \$1,000 in your account and then you earned \$50 of interest, your account is now worth \$1,050. Here's where it gets exciting! From now on, the bank will treat that \$50 of interest as principal. That means you will earn interest on the entire \$1,050 this year, not just on the \$1,000 you initially invested. So how much will your account be worth after the second year?

Interest earned in the second year = $(\$1,050) \times 5\% = \52.50

Account value = $\$1,050 + \$52.50 = \$1,102.50$ after the second year

Notice that you earned more interest in the second year ($\$52.50 > \50) because of the compounding. I know, you're saying, "big whoop, it's only \$2.50 more. Who cares?" Here's why you should care – let's leave that money in the account for the next 40 years. If it earns 5% each year your initial \$1,000 will grow to over \$7,000!! (\$7,040 to be exact). Your money increased by 600% over that 40 years, and all you had to do was sit there and watch it grow. If you could have earned an annual return of 10%, your \$1,000 would have grown to more than \$45,250 over the 40-year period. If that's not worth a "big whoop", I don't know what is!

Here's another reason that time value of money is such a powerful force. Let's assume that you invest \$500 each year into an account that will earn a return of 8%, compounded annually (one time per year). After 5 years your account will be worth \$2,933 – you've invested \$2,500 ($\$500/\text{year} \times 5 \text{ years} = \$2,500$), so you have earned \$433 interest over that time. Now assume that you invest \$500/year for the next 50 years. You will have invested \$25,000 of principal over that time, but your account will have grown to over \$286,000 due to compound interest!! Yes, you read that correctly; your \$25,000 grew to over \$286,000 over that 50-year period. And it's all due to compound interest.

If you are good at math, you will see that compound interest grows exponentially each year. If you aren't good at math, think of it this way – think of a jet airplane taking off from the runway. At first it climbs very slowly (like the \$2.50 increase in interest from above). But as it gains some speed it starts to shoot up into the sky (like the \$286,000!). That is how compound interest works – slow growth for the first 10-15 years, and then it really takes off!

There are a lot of different calculations that we can do with time value of money. We can look at what our money in hand today will grow to in the future. Or we can look at how much we would rather have in hand today instead of waiting to receive money in the future. And lots of other different variations. You already know how to calculate loan payments – that is also a time value of money calculation. But let's just focus on three main uses of time value of money:

Future Value (FV) of a Lump Sum

Present Value (PV) of a Lump Sum

Future Value of an Annuity (FVA)

Wait a minute, there are some terms here that we haven't defined yet. Don't worry, here are the definitions:

Future Value (FV) = what the money you have today will be worth in the future

Present Value (PV) = how much money you would rather have today (the present) instead of waiting to receive money sometime in the future

Lump Sum = a one-time investment; money only changes hands one time

Annuity = a stream of constant payments over a period of time (like loan payments)

There are several ways to calculate time value of money problems:

- Time Value of Money tables (just like the loan factor tables)
- Spreadsheets
- Financial calculators
- Time Value of Money formulas

We are going to focus on using the tables and a spreadsheet. For both methods it is helpful to develop a chart of information. This will help you identify the information that you know, and it will also help you determine what you are solving for.

Future Value of a Lump Sum

Like the name says, we use Future Value of a Lump Sum to determine how much the money you invest today (and today only) will be worth in the future. The example of calculating what your \$1,000 investment today (and today only) would grow to after 40 years is a Future Value of a Lump Sum problem. We use Table 1 Future Value of a Lump Sum for these calculations. The tables are set up exactly the same as the annual loan payment table you used in the previous module – find the column with your interest rate (rate of return) and the row with the number of periods to determine the FV factor. The easiest way to learn is to work some problems.

Example 1. George wants to invest \$5,000 in an account that will earn a 6% annual rate of return (interest rate). How much will he have in his account 10 years from now? First, let's build a chart of the information:

N = Number of periods

I = Interest rate

PV = Present Value, or what you are investing today (lump sum)

PMT = Payment, or how much you will be investing or receiving every period (annuity)

FV = Future Value, or what your account will be worth in the future (lump sum)

N = 10 years

I = 6% per year (this needs to be in the same units as N. In this case, both are in "years")

PV = \$5,000 lump sum invested today
PMT = \$0 (George is not making or receiving payments each year other than the interest)
FV = ?? This is what we are solving for

Using Table 1, the FV factor for 6% for 10 years is 1.7908. We calculate the FV of the lump sum by multiplying the PV by the factor:

$$\text{FV of Lump Sum} = \$5,000 \times 1.7908 = \$8,954$$

George's \$5,000 investment will grow to \$8,954. He will earn interest worth \$3,954 (\$8,954 - \$5,000) over this 10-year period.

To solve this problem using the spreadsheet, open the Lesson 8 TVM Calculator spreadsheet and click on the "FV Calculator" worksheet (at the bottom of the screen). Then, you simply enter the information from your chart into the spreadsheet.

Number of Years (N) = 10
Annual Rate (I) = 6%
Present Value (PV Lump Sum) = \$5,000
Payment to be Made (PMT or Annuity) = \$0

The END or BGN (0/1) is not needed for lump sum calculations; you only need to worry about this for PMT problems. END means that the payments are made at the end of the period. BGN means that the payments are made at the beginning of the period (starting today).

When you enter the information into the spreadsheet you will see the Future Value is automatically calculated. The result is \$8,954.24. The spreadsheet will give you more accurate answers than the tables because the tables round off the factors to 4 decimal places; the spreadsheet does not round the factors at all.

The nice part of using the spreadsheet is that you can change one factor at a time to see how your answer will change. Change N to 40 years to see what George's account will be worth at the end of 40 years. Wow! It'll be worth \$51,428.59

Example 2. Let's look at the impact of inflation. Current gasoline prices are around \$2.00/gal. What will the price of gas be in 15 years if prices increase (inflate) at a rate of 4% each year?

N = 15 years
I = 4% per year
PV = \$2.00 (current price of gas)
PMT = \$0 (we aren't making any other payments)
FV = ??

Using Table 1, we can see the FV factor for 4% and 15 years is 1.8009. So we can estimate the future gas price to be:

$$\text{FV of Gas Price} = \$2.00/\text{gal} \times 1.8009 = \$3.60/\text{gal in 15 years}$$

Present Value of a Lump Sum

This is the opposite of FV of a Lump Sum. The only difference is that we will use Table 2 or the “PV Calculator” of the spreadsheet. PV of a Lump Sum calculates how much money you would rather have in hand today instead of waiting to receive money in the future. Another way to use PV of a lump sum is to determine how much you need to invest today to reach a certain goal (for example, a down payment on a house). This is also an excellent way of determining the maximum you should be willing to pay for something today.

Example 3. You want to have \$20,000 in an account for a down payment on a house at the end of 10 years. Your account earns 5% annually. How much do you need to invest today to reach your goal of \$20,000 after 10 years?

- N = 10 years
- I = 5% per year (the annual inflation rate)
- PV = ?? (this is what we are solving for)
- PMT = \$0 (we aren't making any other payments)
- FV = \$20,000 (what we want to have)

Using Table 2 we see that the PV factor for 5% for 10 years is 0.6139. To calculate how much we have to invest today to reach our goal, simply multiply the FV by the factor:

$$\text{PV to Invest Today} = \$20,000 \times 0.6139 = \$12,278$$

If you were to invest \$12,278 today, it would grow to \$20,000 after 10 years.

Example 4. Mary thinks that a certain piece of land will be worth \$10,000/acre at the end of 5 years. She wants to purchase the land, but only if she can earn a profit (return) of 8% per year. What is the maximum that Mary can afford to pay for this land today?

- N = 5 years
- I = 8% per year (the annual rate of return she wants to earn)
- PV = ??
- PMT = \$0
- FV = \$10,000 (what Mary expects the land to be worth)

Using Table 2, the factor for 8% for 5 years is 0.6806. This means that the maximum price that Mary can afford to pay for the land is:

$$\text{Maximum Purchase Price} = \$10,000 \times 0.6806 = \$6,806/\text{acre}$$

Mary can earn an 8% rate of return on this land if she pays less than \$6,806/acre. Pretty neat, huh?! Now, use the spreadsheet to determine the maximum purchase price if Mary wants to earn a 5% rate of return.

You can always double-check your answers in time value of money problems by working backwards. For example, if you are working a Present Value question, you can use Future Value to check your answer (and the other way around!). Let's do this for Mary's example. We have calculated that the maximum purchase price (the PV) is \$6,806/acre if she wants to earn an 8% return. To double-check this answer, let's use the \$6,806 as the PV and solve for the FV.

$$N = 5$$

$$I = 8\%$$

$$PV = \$6,806 \text{ (the PV you just calculated)}$$

$$PMT = \$0$$

$$FV = ?? \text{ (your answer should be very close to } \$10,000, \text{ the FV from the original situation)}$$

The FV factor for 8% for 5 years is 1.4693. So the future value of the property should be:

$$FV = \$6,806 \times 1.4693 = \$10,000 \quad \text{It works!!}$$

Future Value of an Annuity

An annuity is a constant payment over a certain number of years. A great example would be investing money for a down payment on a house, or for your retirement. The difference between annuities (payments) and lump sums is that with annuities you are making (or receiving) a payment every year; with lump sums you are only investing money one time. The process of calculating the Future Value of an Annuity (FVA) is exactly the same as above. Simply multiply the annual payment you are making by the FVA factor. Here are some examples:

Example 5. Greta's business has been successful, so she has money that she wants to invest for her retirement. She thinks she can invest \$5,000/year for the next 30 years. Her investment should earn an annual return of 7%. How much money will Greta have in her retirement account at the end of 30 years?

$$N = 30 \text{ years}$$

$$I = 7\% \text{ per year}$$

$$PV = \$0 \text{ (there is no lump sum, only payments)}$$

$$PMT = \$5,000 \text{ per year}$$

$$FV = ??$$

Use Table 6 Future Value of Annuity Factors to get the correct factor. For 7% over 30 years the factor is 101.0730. So, if Greta invests \$5,000/year for the next 30 years her retirement account will have:

$$FVA = \$5,000 \times 101.0730 = \$505,365$$

This can't be correct, can it? She only invested \$150,000 (\$5,000/year x 30 years). How can it grow to over \$500,000? The answer is "compound interest". And an important thing for you to remember is that "time is on your side." The earlier you can start investing for a goal, the less money you actually need to invest!

Here's a good place to talk about the END and BGN cells in the TVM Calculator spreadsheet. END indicates that you wait until the end of the period to make your payments. Rather than making the first payment today you will wait until the end of the year to make that first payment. BGN (Beginning) indicates that you will start making payments today, and at the beginning of every period. You will end up with more money over time if you make your payments at the beginning of each period because you will have one more period of compound interest on your side. Just so you know, the Future Value of Annuity Factor table (Table 6) assumes that all payments are made at the beginning of each period.

Use the spreadsheet to see how big of a difference it will make if Greta makes either END or BGN payments. Here's how you do it. Let's start with BGN payments:

N = 30 years
I = 7% per year
PV = \$0
PMT = \$5,000 per year
END or BGN = 1 (use 1 for BGN payments; use 0 for END payments)
FV = \$505,365.21 (the same answer we got using factor)

To look at END payments, simply change the END or BGN cell to 0 (zero).

N = 30 years
I = 7% per year
PV = \$0
PMT = \$5,000 per year
END or BGN = 0 (use 1 for BGN payments; use 0 for END payments)
FV = \$472,303.93 (the same answer we got using factor)

Now you can see that Greta will have \$472,303.93 in her retirement account at the end of 30 years – a difference of more than \$33,000 just because Greta waited one year to start investing! Do you see why it is important to start investing today rather than waiting?!

There are lots of other calculations we can do with Time Value of Money, but these examples (along with calculating loan payments) are the most common ones. TVM is a powerful concept that will come in useful to a business manager in many ways!